## Deep Learning - Embedding 深度学习 - 嵌入

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### Word2Vec

#### "You shall know a word by the company it keeps"

(J. R. Firth 1957: 11)

Build a Cooccurance metrix (using a moving window)

- I like deep learning.
- I like NLP.
- I enjoy flying.

counts	1	like	enjoy	deep	learning	NLP	flying	
1	0	2	1	0	0	0	0	0
like	2	0	0	1	0	1	0	0
enjoy	1	0	0	0	0	0	1	0
deep	0	1	0	0	1	0	0	0
learning	0	0	0	1	0	0	0	1
NLP	0	1	0	0	0	0	0	1
flying	0	0	1	0	0	0	0	1
	0	0	0	0	1	1	1	0
•					rel s J low-	'		pve

### Word Embedding

• Map each word to a vector (in relatively low-dim space)

approach 1 SVD/PCA - Some notes: remove "of" "the" (Syntatic Words) - Use Pearson correlations (rather than count)  $P_{XY} = \frac{C_{0V}(X,Y)}{\partial_X \partial_Y} = \frac{E[(X-EX)(I-EY)]}{\sqrt{Var}(X)Var(Y)}$ - set neg velues to zero WRIST CHOOSING CHOOSE ANKLE SHOULDER DRIVER ARM LEG - HAND - FOOT STOLEN HEAD STEAL -+ NOSE OSTOLE - FINGER DSTEALING - TOE JANITOR - FACE SWIMMER O DRIVE - EAF STUDENT EYE TAKE TOOTH ■TAKEN □ TAKING ○ TOOK DOG - PUPPY KITTEN - THREE THREE -+ COW MOUSE **OCLEAN** TEACHER OYSTER -+ LION DOCTOR BULL - CHICAGO BRIDE - ATLANTA SWIM EATENT MONTREAL PRIEST → NASHVILLE SHOWING - TOKYO CHINA - RUSSIA SHOW AFRICA OTEACH ASIA OLEARN GROWN GROWN EUROPE OMARB - AMERICA OGREW - BBAZIL - MOSCOW -+ FRANCE HAWAI OPRAY OTREAT GROWING Problem: SVD expensive for large Vocabulary special algorithm ( doesn't fit into DL pipeline )

### Word2Vec

word 2 Vec (Mikolov et al. 2013)

Predict Shrrounding words in a window (of len m) of every word Wt Wt-m WEHM m m First define a probabilistic model each word w has two vectors I w (the embedding of w when w is outside) We want to learn  $\mathcal{U}_{\mathcal{W}}$ .  $\mathcal{V}_{\mathcal{W}}$  for  $\mathcal{W} \in \mathcal{W}$  $\frac{P(O|C)}{1} = \frac{\exp(\langle \mathcal{U}_{o}, \mathcal{V}_{c} \rangle)}{\sum_{w=1}^{n} \exp(\langle \mathcal{U}_{w}, \mathcal{V}_{c} \rangle)} \leq \text{ softmax}/\log istic regression}$ Mur 7 Mo if Mo Ve in the same direction. P(O(c) is large.

### Objective of Word2Vec



training: 
$$\nabla \log P(W_0 | W_c)$$
 is expensive  $(O(W) + the)$   
 $\square$  Rierarchical Softmax  $(it is an approximation)$   
 $(\square Rierarchical Softmax  $(it is an approximation)$   
 $(\square (W_0)) = jth node on the root  $\rightarrow W$  path  
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 $(\square (W_0)) = (\square (W_0)) = jth (W_0) =$$$$ 

### Training method 2



• 
$$X_{apple} - X_{apples} \approx X_{car} - X_{cars} \approx X_{family} - X_{families}$$
  
•  $X_{shirt} - X_{clothing} \approx X_{chair} - X_{furniture}$   
•  $X_{king} - X_{man} \approx X_{queen} - X_{woman}$   
a:b::c:?  
 $d = \arg \max_{x} \frac{(w_{b} - w_{a} + w_{c})^{T} w_{x}}{||w_{b} - w_{a} + w_{c}||}$   
 $w_{b}$   
 $w_{b}$   
 $w_{b} - w_{a} + w_{c}$   
 $w_{b} - w_{a} + w_{c}$   
 $w_{b} - w_{a} + w_{c}$   
 $w_{b} - w_{a} + w_{c}$ 

### Notes

- Word2Vec: unsupervised learning
  - Huge amount of training data (no label is needed)
- Can be incorporated to deep learning pipeline
  - The corresponding layers is usually called the embedding layer
  - The resulting vectors obtained from word2vec can be used to initialize the parameters of NN
  - We can also get the embedding from training a specified DNN (for a specific task)
    - Computational complexity too high (much higher than word2vec)
    - The embedding may not be useful in other tasks
    - On the other hand, word2vec captures a lot of semantic information, which is useful in a variety of tasks

According to Mikolov:

CBOW (Continuous Bag of Words): Use context to predict the current word.

--several times faster to train than the skip-gram, slightly better accuracy for the frequent words Skip-gram: Use the current word to predict the context.

--works well with small amount of the training data, represents well even rare words or phrases.

### GloVe

GloVe: Global Vectors for Word Representation

predicting the context given a word

### Ratio Matters



$$\begin{array}{c|c|c|c|} P(k|steam) & 8.9 & 8.5 \times 10^{-2} & 1.36 & 0.96 \\ \hline & & & & \\ \hline \hline & & & \\ \hline \hline \\ \hline & & & \\ \hline \hline \\ \hline \hline & & & \\ \hline \hline \\ \hline \hline \\ \hline \hline \hline \\ \hline \hline \\ \hline \hline \hline \\ \hline \hline \hline \hline \\ \hline \hline \hline \hline \\ \hline \\ \hline \hline$$

### Derivation

Define  $F(w_i, w_j, \widetilde{w}_k) = \frac{P_{ik}}{P_{jk}}$ Using the property of F, we try to derive the form of  $\langle w_i, \tilde{w}_k \rangle$ want  $\mathbb{D}F(W_i, W_j, \widetilde{W}_k) = F(\langle W_i - W_j, \widetilde{W}_k \rangle)$ Chforce a linear structure @ Imagine we switch the role of a word & a context i.e.  $X \rightarrow X^{\mathsf{T}}$ then we'd better have  $\omega_i \rightarrow \widetilde{\omega}_i$  (symmetric) So we choose F = exp  $\left(\exp\left(\left(\omega_{i}-\omega_{j},\widetilde{\omega}_{k}\right)\right)=\frac{e_{X}p\left(\omega_{i},\widetilde{\omega}_{k}\right)}{e_{X}p\left(\omega_{j},\widetilde{\omega}_{k}\right)}=\frac{P_{i\kappa}}{P_{j\kappa}}=\frac{X_{ik}/X_{i}}{X_{j\kappa}/X_{j}}\right)$  $= \frac{1}{2} \left\{ \begin{array}{c} \langle \omega_{i}, \widetilde{\omega}_{k} \rangle + b_{i} + \widetilde{b}_{k} \rangle = \log \left( X_{ik} \right) & \log X_{i} \\ \langle \omega_{i}, \widetilde{\omega}_{k} \rangle + b_{i} + \widetilde{b}_{k} \rangle = \log \left( \frac{X_{ik}}{X_{jk}} \right) - \left( b_{j} - b_{j} \right) \\ \left( Venify \langle \omega_{i} - \omega_{j}, \widetilde{\omega}_{k} \rangle = \log \left( \frac{X_{ik}}{X_{jk}} \right) - \left( b_{j} - b_{j} \right) \\ \text{We try to factorize } \log X \quad \left( i.e., w \left( \frac{d}{2} \right) \left( \widetilde{\omega} \right) = \log \left( \frac{1}{2} \right) \\ \end{array} \right)$ 

### Objective



**Glove Visualizations: Superlatives** 



#### **Glove Visualizations: Company - CEO**



### **Glove results**

Nearest words to frog:

- 1. frogs
- 2. toad
- 3. litoria
- 4. leptodactylidae
- 5. rana
- 6. lizard
- 7. eleutherodactylus



litoria





#### leptodactylidae



#### eleutherodactylus

### Reference

- Baroni, Marco, Georgiana Dinu, and Germán Kruszewski. Don't count, predict! A systematic comparison of context-counting vs. context-predicting semantic vectors. ACL 14
  - An early paper claims that the prediction formulation (like word2vec) is better than factorizing a co-occurrence matrix
- Levy, O., Goldberg, Y., & Dagan, I. (2015). Improving Distributional Similarity with Lessons Learned from Word Embeddings.

(comparing several SNSG, GloVe, and SVD)

A very reasonable blog discussing the relations between different models

http://sebastianruder.com/secret-word2vec/index.html

- O Levy, Y Goldberg. Neural Word Embedding as Implicit Matrix Factorization. NIPS 14. (in blackboard)
- Network Embedding as Matrix Factorization: Unifying DeepWalk, LINE, PTE, and node2vec. Jiezhong Qiu, Yuxiao Dong, Hao Ma, Jian Li, Kuansan Wang, Jie Tang. The 11th ACM International Conference on Web Search and Data Mining (WSDM 2018).

### Deep Walk -embedding node in a social network

### Embedding node (using pairwise relations)



(a) Input: Karate Graph

(b) Output: Representation

### Key Idea

### treat vertex as words, random walks as sentences



<b>Algorithm 2</b> SkipGram( $\Phi$ , 1	$\mathcal{V}_{v_i}, w)$										
1: for each $v_j \in \mathcal{W}_{v_i}$ do	- look at each vertex in the random welk Uj										
2: for each $u_k \in \mathcal{W}_{v_i}[j-w:j+w]$ do $\leftarrow$ used in the used in the sinder											
3: $J(\Phi) = -\log \Pr(u_k)$	$P(v_j)$										
4: $\Phi = \Phi - \alpha * \frac{\partial J}{\partial \Phi}$	Prob of $u_k$ (context word)										
5: end for	j · · · · · · · · · · · · · · · · · · ·										
6: end for											

Use Hierarchical softmax to approximate

# Multimodal representation learning ---Image Caption 2

Kires et al. Unifying Visual-Semantic Embeddings with Multimodal Neural Language Models



there is a cat sitting on a shelf.



a plate with a fork and a piece of cake .



a black and white photo of a window .



a young boy standing on a parking lot next to cars.





a kitchen with stainless steel appliances.



a giraffe is standing next to a fence in a field . (hallucination)



this is a herd of cattle out in the field .



trying to be seen in the water . (counting)



a car is parked in the middle of nowhere .



a parked car while driving down the road . (contradiction)



a ferry boat on a marina with a group of people.



the handlebars are trying to ride a bike rack . (nonsensical)





a little boy with a bunch of friends on the street .



a woman and a bottle of wine in a garden . (gender)

Figure 1: Sample generated captions. The bottom row shows different error cases. Additional results can be found at http://www.cs.toronto.edu/~rkiros/lstm\_scnlm.html

### Overview



Figure 2: Encoder: A deep convolutional network (CNN) and long short-term memory recurrent network (LSTM) for learning a joint image-sentence embedding. Decoder: A new neural language model that combines structure and content vectors for generating words one at a time in sequence.





bowl

(d) Sanity check

- box + bow| =

(c) Image structure





Figure 5: PCA projection of the 300-dimensional word and image representations for (a) cars and colors and (b) weather and temperature.

### Details

#### • LSTM notations used in this work

Let  $X_t$  denote a matrix of training instances at time t. In our case,  $X_t$  is used to denote a matrix of word representations for the t-th word of each sentence in the training batch. Let  $(I_t, F_t, C_t, O_t, M_t)$  denote the input, forget, cell, output and hidden states of the LSTM at time step t. The LSTM architecture in this work is implemented using the following equations:

$$\mathbf{I}_{t} = \sigma(\mathbf{X}_{t} \cdot \mathbf{W}_{xi} + \mathbf{M}_{t-1} \cdot \mathbf{W}_{hi} + \mathbf{C}_{t-1} \cdot \mathbf{W}_{ci} + \mathbf{b}_{i})$$
(1)

$$\mathbf{F}_{t} = \sigma(\mathbf{X}_{t} \cdot \mathbf{W}_{xf} + \mathbf{M}_{t-1} \cdot \mathbf{W}_{hf} + \mathbf{C}_{t-1} \cdot \mathbf{W}_{cf} + \mathbf{b}_{f})$$
(2)

$$\mathbf{C}_{t} = \mathbf{F}_{t} \bullet \mathbf{C}_{t-1} + \mathbf{I}_{t} \bullet tanh(\mathbf{X}_{t} \cdot \mathbf{W}_{xc} + \mathbf{M}_{t-1} \cdot \mathbf{W}_{hc} + \mathbf{b}_{c})$$
(3)

$$\mathbf{O}_t = \sigma (\mathbf{X}_t \cdot \mathbf{W}_{xo} + \mathbf{M}_{t-1} \cdot \mathbf{W}_{ho} + \mathbf{C}_t \cdot \mathbf{W}_{co} + \mathbf{b}_o)$$
(4)

$$\mathbf{M}_t = \mathbf{O}_t \bullet tanh(\mathbf{C}_t) \tag{5}$$

where  $(\sigma)$  denotes the sigmoid activation function,  $(\cdot)$  indicates matrix multiplication and  $(\bullet)$  indicates component-wise multiplication. <sup>1</sup>

### Details

Let  $\mathbf{q} \in \mathbb{R}^D$  denote an image feature vector

• D: length of the CNN code (CNN can be AlexNet, VggNet, or ResNet)

 $\mathbf{x} = \mathbf{W}_I \cdot \mathbf{q} \in \mathbb{R}^K$  be the image embedding.

image description  $S = \{w_1, \ldots, w_N\}$  with words  $w_1, \ldots, w_N$ 

 $\{\mathbf{w}_1, \ldots, \mathbf{w}_N\}, \mathbf{w}_i \in \mathbb{R}^K, i = 1, \ldots, n$  denote the corresponding word representations to words  $w_1, \ldots, w_N$  (entries in the matrix  $\mathbf{W}_T$ ). The representation of a sentence  $\mathbf{v}$  is the hidden state of the LSTM at time step N (i.e. the vector  $\mathbf{m}_t$ ).

 $W_T$ : precomputed using e.g. word2vec



### Details

• Optimize pairwise rank loss ( $\theta$ :parameters needed to be learnt:  $W_I$  and LSTM parameters) (similar to negative sampling in spirit)



 $\mathbf{v}_k$  is a contrastive (non-descriptive) sentence for image embedding  $\mathbf{x}$ , and vice-versa with  $\mathbf{x}_k$ .